



**EDUCATIONAL QUALITY AND
ASSESSMENT PROGRAMME**



***Scoring
Rubric
2020***

**South Pacific
Form
Seven
Certificate**

M

A

T

H

S

WITH

C

A

L

C.

© Educational Quality and Assessment Programme, 2020

3 Luke Street, Nabua, Private Mail Bag, Suva, Fiji.

Telephone: (679) 3370733 Fax: (679) 3370021

All rights reserved. No part of this publication may be reproduced by any means without the prior permission of the Educational Quality and Assessment Programme

Strand: 1 ALGEBRA

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
1.1	1	Simplify $4x - 8 = 5(x+2) - x$ $\rightarrow 4x - 8 = 2x + 10 - x$ $\rightarrow 4x - 8 = x + 10$ $\rightarrow 4x - x = 10 + 8$ $\rightarrow 3x = 18$ $\rightarrow \therefore \boxed{x=6}$	Final Answer. Allow for slips			
1.2	1	Points of intersection $y=y$ $y+3=x$ $3x+y=1$ Method 1 (Substitution) $y=x-3$ $3x+(x-3)=1$ $y(1)-3$ $4x=1+3$ $\boxed{y=-2}$ $4x=4$ $\boxed{x=1}$	Final Answer: $(1, -2)$ Allow for slips If student has shown evidence of doing either steps correctly, but made minor algebraic errors to get the answer Compensate their effort, Even though they might Get 1 wrong.	Method 2 (Elimination) $y + 3 = x$ $3x + y = 1$ $3x + y = 1$ $y - x = -3$ $-(-x + y = -3)$ $y - 1 = -3$ $4x =$ 4 $y = -3 + 1 = -2$ $x =$ $4/4 = 1$		
1.3	1	$\frac{x+1}{2} \leq \frac{4-x}{-3}$ $\rightarrow -3(x+1) \geq 2(4-x)$ $\rightarrow -3x-3 \geq 8-2x$ $\rightarrow -3x+2x \geq 8+3$ $\rightarrow -x \geq 11$ $\rightarrow x \leq \frac{11}{-1}$ $\rightarrow \boxed{x \leq -11}$	Final Answer. Check to see that the inequality sign has been reversed TWICE, when multiplying/dividing by a negative number.			
1.4	1	$\frac{\sqrt{2-p}}{3} = x+1$ $\rightarrow \sqrt{2-p} = 3(x+1)$ $\rightarrow 2-p = (3x+3)^2$ $\rightarrow 2 = (3x+3)^2 + p$ $\therefore \boxed{p = 2 - (3x+3)^2}$	Final Answer. Quadratic factor can be accepted in Crude form/ does not need to be expanded, Possible solutions: \rightarrow	$p = 2 - (3x+3)^2$ $p = 2 - (9x^2 + 18x + 9)$ $p = 2 - 9x^2 - 18x - 9$ $p = -9x^2 - 18x - 7$	$2-p = (3x+3)^2$ $-p = (3x+3)^2 - 2$ $p = \frac{(3x+3)^2 - 2}{-1}$	

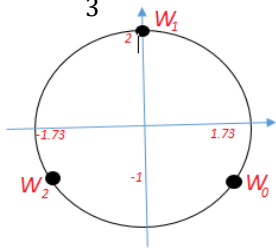
Strand: 1 ALGEBRA

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
1.5	1	Factorise $x^2 - 15x + 26$ $\rightarrow (x - 13)(x - 2)$	Final Answer.			
1.6	1	Factorise $2x^2 - 7x + 3 = 0$ $\rightarrow (2x - 1)(x - 3) = 0$ $\rightarrow 2x - 1 = 0$ $x - 3 = 0$ $\rightarrow X = \frac{1}{2}$ $X = 3$	Final Answer. Possible solution is the usage of the Quadratic Formula to solve:	$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(2)(3)}}{2(2)}$ $x = \frac{7 \pm \sqrt{49 - 24}}{4} = \frac{7 \pm \sqrt{25}}{4}$ $x = \frac{7 \pm 5}{4} \rightarrow x_1 = \frac{12}{4} = 3 \quad x_2 = \frac{1}{2}$		
1.7	1	$\frac{(p^2)^n \times p^{4n} \times p}{p^{5n}}$ $\frac{p^{2n} \times p^{4n} \times p^1}{p^{5n}}$ $\frac{p^{6n} \times p^1}{p^{5n}}$ $\frac{p^{6n+1}}{p^{5n}}$ $p^{6n+1-5n} = \boxed{p^{n+1} \text{ OR } p^n \cdot p}$	Final Answer. Allow for slips Reward if Laws of Indices used $(p^2)^n = p^{2n}$ $p^{2n} \cdot p^{4n} \cdot p^1 = p^{6n+1}$ $\frac{p^{6n+1}}{p^{5n}} = p^{6n+1-5n}$			
1.8	1	$x^3 - 13x^2 - 50x - 56$ by $(x - 7)$ $x - 7 \overline{) \begin{array}{r} x^3 - 13x^2 - 50x - 56 \\ -(x^3 - 7x^2) \\ \hline -6x^2 - 50x \\ -(-6x^2 + 42x) \\ \hline -92x - 56 \\ -(-92x + 644) \\ \hline -700 \end{array}}$ $x^2 - 6x - 92 + \frac{-700}{x - 7}$	Final Answer. Alternate answer is to use Synthetic Division.	<p>Synthetic Division only uses coefficients</p> $\begin{array}{r rrrr} & 7 & -42 & -644 & \\ 7 & 1 & -13 & -50 & -56 \\ & & 1 & -6 & -92 & -700 \rightarrow \\ \hline & & & & & \text{Remainder} \\ & & & & & x^2 - 6x - 92 + \frac{-700}{x - 7} \end{array}$		
1.9	1	$3x^2 + ax - 4 = 5$ $(x + 3) = 0 \rightarrow x = -3$ <u>Substitute x=-3</u> $3(-3)^2 + a(-3) - 4 = 5$ $3(9) - 3a - 4 = 5$ $27 - 3a - 4 = 5$ $23 - 3a = 5$ $23 - 5 = 3a$ $18 = 3a$ $\therefore a = 6$	Final Answer			

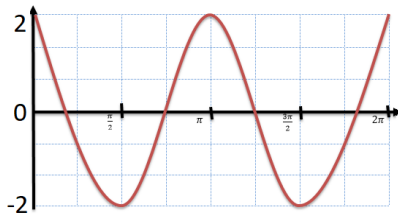
Strand: 1 ALGEBRA

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
1.10	1	$\binom{3}{0}(x)^3\left(-\frac{1}{x}\right)^0 = (1)x^3(1) = x^3$ $\binom{3}{1}(x)^2\left(-\frac{1}{x}\right)^1 = (3)x^2\left(-\frac{1}{x}\right) = -3x$ $\binom{3}{2}(x)^1\left(-\frac{1}{x}\right)^2 = (3)x^1\left(\frac{1}{x}\right)^2 = \frac{3}{x}$ $\binom{3}{3}(x)^0\left(-\frac{1}{x}\right)^3 = (1)(1)\left(-\frac{1}{x}\right)^3 = -\frac{1}{x^3}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $x^3 - 3x + \frac{3}{x} - \frac{1}{x^3}$ </div>	Final Answer. Allow for slips			
1.11	1	$2\sqrt{3} + 4\sqrt{3} - \sqrt{27}$ $\rightarrow 2\sqrt{3} + 4\sqrt{3} - \sqrt{9}\sqrt{3}$ $\rightarrow 2\sqrt{3} + 4\sqrt{3} - 3\sqrt{3}$ $\rightarrow (2 + 4 - 3)\sqrt{3}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $= 3\sqrt{3}$ </div>	Final Answer. Allow for slips in + or - of surds Reward students who were able: \rightarrow To break $\sqrt{27} = 3\sqrt{3}$ \rightarrow To get $7\sqrt{3} - \sqrt{27}$			
1.12	1	$\frac{(1 + 2x)}{3} - \frac{5x}{2} = \frac{(x - 3)}{4}$ $\rightarrow \frac{2(1+2x) - 3(5x)}{6} = \frac{(x-3)}{4}$ $\rightarrow \frac{2+4x-15x}{6} = \frac{(x-3)}{4}$ $\rightarrow \frac{2-11x}{6} = \frac{(x-3)}{4}$ $\rightarrow 4(2 - 11x) = 6(x - 3)$ $\rightarrow 8 - 44x = 6x - 18$ $\rightarrow 8 + 18 = 6x + 44x$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $\therefore x = \frac{26}{50} = \frac{13}{25} = 0.52$ </div>	Final Answer. Allow for slips Check for LCD of "6" Cross-multiplication Alternate Solution is to multiply the whole equation by 24 or 12 - to remove the denominators.	<div style="border: 1px solid black; padding: 5px;"> <p style="text-align: center; margin: 0;">ALTERNATE SOLUTION (multiplying by a factor 12 or 24)</p> $\frac{12x(1 + 2x)}{3} - \frac{12x \cdot 5x}{2} = \frac{12x(x - 3)}{4}$ $4(1 + 2x) - 6(5x) = 3(x - 3)$ $4 + 8x - 30x = 3x - 9$ $4 + 9 = 3x + 22x$ $\therefore x = \frac{13}{25} \approx 0.52$ </div>		
1.13	1	$\left(\frac{(2x)^3 \cdot y^{-4}}{6x^5 \cdot y^{-7}}\right)^{-2} = \left(\frac{6x^5 \cdot y^{-7}}{(2x)^3 \cdot y^{-4}}\right)^2$ $= \left(\frac{6x^5 \cdot y^4}{8x^3 \cdot y^7}\right)^2$ $= \left(\frac{3x^2}{4y^3}\right)^2$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $= \frac{9x^4}{16y^9}$ </div>	Final Answer. Allow for slips Check for the inversion/reciprocal Of the fraction that will make exterior power POSITIVE			

Strand: 1 ALGEBRA

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
1.14	1	$\begin{aligned} x^2 - 16x + k \\ (x - a)^2 \rightarrow \frac{-16}{2} = -8 \\ (x - 8)^2 = x^2 - 16x + 64 \\ \therefore k = 64 \end{aligned}$	Final Answer			
1.15	2	$\begin{aligned} \frac{v}{u} &= \frac{r_1}{r_2} \text{cis}(\theta_1 - \theta_2) \\ \frac{v}{u} &= \frac{8}{2} \text{cis}\left(\frac{\pi}{2} - \frac{\pi}{3}\right) \\ \frac{v}{u} &= 4 \text{cis}(90 - 60) \\ \frac{v}{u} &= 4 \text{cis}(30) \text{ or } 4 \text{cis} \frac{\pi}{6} \\ \frac{v}{u} &= 4 \left(\frac{\sqrt{3}}{2} + \frac{1}{2}i\right) = 2\sqrt{3} + 2i \\ &= 3.46 + 2i \end{aligned}$	Answer in polar form $4 \text{cis}(30)$ or $4 \text{cis} \frac{\pi}{6}$	Final Answer in Rectangular Form $2\sqrt{3} + 2i$ Or $3.46 + 2i$		
1.16	4	$\begin{aligned} W &= 8 \left(\cos -\frac{\pi}{2} + i \sin -\frac{\pi}{2}\right) \\ W^3 &= -8i = 8 \text{cis} -90 \\ \text{Angles} \\ \theta &= \frac{360}{3} = 120^\circ \text{ apart.} \\ \theta_1 &= \frac{-90}{3} = -30^\circ \text{ or } 330^\circ \\ \theta_2 &= -30 + 120 = 90^\circ \\ \theta_3 &= 90 + 120 = 210^\circ \\ r &= \sqrt[3]{8} = 8^{\frac{1}{3}} = 2 \\ W_0 &= 2 \text{cis} -\frac{\pi}{6} = 2 \text{cis} -30^\circ \\ W_1 &= 2 \text{cis} \frac{\pi}{2} = 2 \text{cis} 90^\circ = 2i \\ W_2 &= 2 \text{cis} \frac{2\pi}{3} = 2 \text{cis} 210^\circ \end{aligned}$ 	Able to find the "r" value of 2, or the usage of De Moivre's Theorem Correct angle θ $W = r^{1/n} \text{cis}\left(\frac{\theta}{n} + \frac{2\pi k}{n}\right)$ $W = 2 \text{cis}\left(\frac{\theta_0}{3} + \frac{2\pi k}{3}\right)$	Was able to get at least one or two roots correct. Argand Diagram is incorrect. Or not drawn. Three Roots in Rectangular Form $W_0 = 1.73 - i$ $W_1 = 2i$ $W_2 = -1.73 - i$	Was able to get all three roots correct. Argand Diagram not drawn/incorrect, Allow for slips If all working is correct and Argand Diagram is drawn - but with only wrong ANGLE/wrong R Value.	All 3 roots correct. Argand Diagram Correct.

Strand: 2 TRIGNOMETRY

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
2.1a	1	$\sec x + \tan x = \frac{1 + \sin x}{\cos x}$ <p>LHS $\frac{1}{\cos x} + \frac{\sin x}{\cos x}$</p> $\frac{1 + \sin x}{\cos x} = \text{RHS}$	<p>Final Answer.</p> <p>Able to write down reciprocal identities:</p> $\sec x = \frac{1}{\cos x}$ $\tan x = \frac{\sin x}{\cos x}$			
2.1b	2	$(1 + \cot^2 \theta)(1 - \cos^2 \theta) \equiv 1$ $\operatorname{cosec}^2 \theta \cdot \sin^2 \theta$ $\frac{1}{\sin^2 \theta} \cdot \sin^2 \theta$ $1 = \text{RHS}$	<p>Able to use the trig identities to get:</p> $1 + \cot^2 \theta = \operatorname{csc}^2 \theta$ $1 - \cos^2 \theta = \sin^2 \theta$	Final Answer.		
2.2	2	<p><u>Pythagoras Theorem</u> Find missing length: $h^2 = a^2 + b^2$</p> $(2)^2 = (\sqrt{3})^2 + b^2$ $4 = 3 + b^2$ $4 - 3 = b^2$ $\therefore b = 1$ $\sin 2x = 2 \cdot \sin x \cdot \cos x$ $= 2 \cdot \left(\frac{1}{2}\right) \cdot \left(\frac{\sqrt{3}}{2}\right)$ $= 2 \cdot \left(\frac{\sqrt{3}}{4}\right)$ <div style="border: 1px solid black; padding: 5px; display: inline-block;"> $= \frac{\sqrt{3}}{2}$ </div>	<p>Final Answer.</p> <p>Was able to use the Pythagoras Theorem to get the missing length of "1".</p> <p>Or if you see</p> $\sin x = \frac{1}{2}$			
2.3	1		<p>Final Answer.</p> <p>Correct shape</p> <p>Correct number of waves</p> <p>y-labels not compulsory</p>			

Strand: 2 TRIGNOMETRY

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
2.4	2	$\cos\left(\frac{\pi}{2} + P\right)$ $= \cos\left(\frac{\pi}{2}\right)\cos(P) - \sin\left(\frac{\pi}{2}\right)\sin(P)$ $= (0)\cos(P) - (1)\sin(P)$ $= \boxed{-\sin P}$	<p>Able to employ the Compound Angle Formula:</p> <p>Correct substitution of $A = \frac{\pi}{2}$ or $B = P$</p>	Final Answer		
2.5	3	<p>A=20 Type of Graph: sine Graph</p> $y = A\sin(Bx + C) + D$ <p>T=0.04 $B = \frac{2\pi}{T} = \frac{2\pi}{0.04} = 50\pi$</p> <p>C=0 and D=0</p> $Y = \boxed{20\sin 50\pi}$	<p>Was able to identify the:</p> <p>Amplitude = 20</p> <p>Or the graph is a SINE wave.</p>	<p>Was able to identify the value of B</p> <p>$B = 50\pi$</p>	Final Answer:	

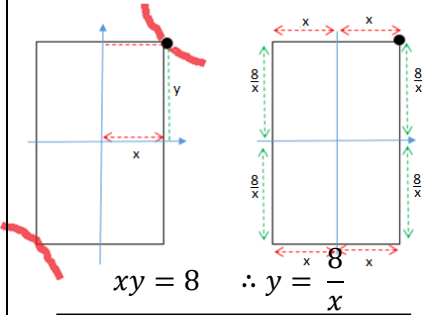
Strand: 3 DIFFERENTIATION

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
3.1	1	<div style="border: 1px solid black; display: inline-block; padding: 5px;"> $x = -1$ </div>	Final Answer			
3.2	2	$\lim_{x \rightarrow 4} \frac{2 - \sqrt{x}}{4 - x}$ $\lim_{x \rightarrow 4} \frac{2 - \sqrt{x}}{4 - x}$ $\lim_{x \rightarrow 4} \frac{(2 - \sqrt{x})}{(2 + \sqrt{x})(2 - \sqrt{x})}$ $\lim_{x \rightarrow 4} \frac{1}{2 + \sqrt{x}}$ $\lim_{x \rightarrow 4} \frac{1}{2 + \sqrt{4}} = \frac{1}{4}$	Was able to use Difference of Two Squares to factorise the denominator into $(2 + \sqrt{x})(2 - \sqrt{x})$	Final Answer.		
<div style="border: 1px solid black; padding: 5px; margin: 10px auto; width: 80%;"> <u>L Hopital's Rule (Alternative Solution)</u> Differentiate : $\frac{-\frac{1}{2}x^{-\frac{1}{2}}}{-1} = \frac{1}{2\sqrt{x}} = \frac{1}{2\sqrt{4}} = \frac{1}{2(2)} = \frac{1}{4}$ </div>						
3.3	1	$\lim_{x \rightarrow \infty} = \frac{(x + 3)(4 - 2x)}{(2x - 5)^2}$ <p style="color: red; margin-left: 20px;">No need to expand whole eqn:</p> $\lim_{x \rightarrow \infty} = \frac{-2x^2}{4x^2}$ $\lim_{x \rightarrow \infty} = \frac{1}{-2}$	Was able to identify the highest term with the HIGHEST POWERS in the numerator OR denominator.	Final Answer		

Strand: 3 DIFFERENTIATION

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
3.4	2	<p>Differentiate : $\frac{e^{2x}}{x+1}$</p> <p>Let $u = e^{2x}$ $\therefore u' = 2e^{2x}$</p> <p>Let $v = x + 1$ $\therefore v' = 1$</p> $\frac{dy}{dx} = \frac{vu^1 - uv^1}{v^2}$ $\frac{dy}{dx} = \frac{(x+1)(2e^{2x}) - (e^{2x})(1)}{(x+1)^2}$ $\frac{dy}{dx} = \frac{2xe^{2x} + 2e^{2x} - e^{2x}}{(x+1)^2}$ $\frac{dy}{dx} = \frac{2xe^{2x} + e^{2x}}{(x+1)^2} +$ $\frac{dy}{dx} = \frac{e^{2x}(2x+1)}{(x+1)^2}$	<p>If any of the terms in the numerator and denominator were differentiated correctly.</p> <p>$\therefore u' = 2e^{2x}$</p> <p>$\therefore v' = 1$</p> <p>If the derivatives were wrong, but was able to recognize this problem employed the Quotient Rule.</p>	<p>Final Answer Allow for slips</p> <p>If the Quotient Rule was used, correctly with the substitution of the terms.</p> <p>Equation does not necessarily need to be simplified or factorized. Reward students, even if they have given it in its Crude Form</p>		
3.5	4	<p>$s(t) = 6t^3 + 2t - \frac{1}{\sqrt{t}}$</p> <p>$s(t) = 6t^3 + 2t - t^{-\frac{1}{2}}$</p> <p><u>1st Derivative:</u></p> <p>$s'(t) = v(t) = 18t^2 + 2 + \frac{1}{2}t^{\frac{1}{2}}$</p> <p><u>2nd Derivative:</u></p> <p>$v'(t) = a(t) = 36t + \frac{1}{4}t^{-\frac{1}{2}}$</p> <p>$a(t) = 36t + \frac{1}{4\sqrt{t}}$</p> <p><u>Acceleration at time t=4sec</u></p> <p>$a(4) = 36(4) + \frac{1}{4\sqrt{4}} = 144 + \frac{1}{8}$</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $= 144.125 \text{ or } \frac{1153}{8} \text{ m/s}^2$ </div>	<p>Was able to write $-\frac{1}{\sqrt{t}}$ as $-t^{-\frac{1}{2}}$</p> <p>Able to show any signs of differentiation.</p> <p>Substituted $t = 4\text{sec}$ into a formula that was differentiated incorrectly.</p>	<p>Was able to differentiate the distance once correctly.</p> <p><u>1st Derivative</u></p> <p>$18t^2 + 2 + \frac{1}{2}t^{\frac{1}{2}}$</p>	<p>Was able to differentiate the distance twice correctly.</p> <p><u>2nd Derivative:</u></p> <p>$36t + \frac{1}{4}t^{-\frac{1}{2}}$</p>	Final Answer.

Strand: 3 DIFFERENTIATION

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
3.6	4	 <p style="text-align: center;">$xy = 8 \quad \therefore y = \frac{8}{x}$</p> <div style="border: 1px solid black; padding: 5px; margin: 5px 0;"> $\text{Perimeter} = 4x + 4 \cdot \left(\frac{8}{x}\right)$ $P = 4x + \frac{32}{x}$ </div> <p>Differentiate</p> $P' = 4 - 32x^{-2}$ <div style="border: 1px solid green; border-radius: 10px; padding: 5px; margin: 5px 0; display: inline-block;"> $Minimum \rightarrow P' = 0$ </div> $0 = 4 - 32x^{-2}$ $32x^{-2} = 4$ $32 = 4x^2$ $8 = x^2$ <div style="border: 1px solid black; padding: 5px; margin: 5px 0; display: inline-block;"> $\therefore x = \sqrt{8} \text{ or } 2\sqrt{2} \text{ or } 2.83$ </div> $\text{Perimeter} = 4x + \frac{32}{x}$ $= 4(\sqrt{8}) + \frac{32}{\sqrt{8}}$ $= 4(\sqrt{8}) + 4(\sqrt{8})$ <div style="border: 1px solid black; padding: 5px; margin: 5px 0; display: inline-block;"> $= 8(\sqrt{8}) \text{ or } 22.63m$ </div>	<p>Was able to write the Perimeter in terms of "x".</p> $\text{Perimeter} = 4x + 4 \cdot \left(\frac{8}{x}\right)$ $P = 4x + \frac{32}{x}$ <p>Was able to make y the subject of the formula:</p> $\therefore y = \frac{8}{x}$ <p>Evidence of any differentiation, even though the equation is wrong.</p>	<p>Able to differentiate the Perimeter equation correctly.</p> $P' = 4 - 32x^{-2}$	<p>Was able to differentiate correctly and equate to zero</p> <p style="text-align: center;">Minimum</p> $P' = 0$ <p>And solve for x</p> $x = \sqrt{8}$ <p style="text-align: center;">or $2\sqrt{2}$</p> <p style="text-align: center;">or 2.83</p>	<p>Final Answer</p> <p>Perimeter given.</p> <p style="text-align: center;">$8(\sqrt{8})$</p> <p style="text-align: center;">or 22.63m</p> <p>Allow for slips</p> <p>If they differentiated correctly, but when solving for x, there answer is wrong – and they substituted the wrong x-value into the Perimeter formula – Reward them with FULL scores.</p>

Strand: 4 INTEGRATION

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
4.1	1	$\int \sqrt{x} + 1 \, dx = \int x^{\frac{1}{2}} + 1 \, dx$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $= \frac{x^{\frac{3}{2}}}{\frac{3}{2}} + x + c$ $= \frac{2}{3} x^{\frac{3}{2}} + x + c$ </div>	<p>Final Answer Allow for slips</p> <p>Do not penalize anyone, if the coefficient is not reciprocated or C is missing.</p>			
4.2	1	$\int 2e^{2x+2} \, dx = \frac{2e^{2x+2}}{2} + C$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $= e^{2x+2} + C$ </div>	<p>Final Answer. Do not penalize if C is missing.</p>			
4.3	2	<p>Find $\int_1^2 3x^2 + 2x - 1 \, dx$</p> $= \left[\frac{3x^3}{3} + \frac{2x^2}{2} - x \right]_1^2$ $= [x^3 + x^2 - x]_1^2$ $= [(2)^3 + (2)^2 - (2)] - [(1)^3 + (1)^2 - (1)]$ $= [8 + 4 - 2] - [1 + 1 - 1]$ $= [10] - [1]$ $= 9$	<p>Was able to integrate the function into</p> $\left[\frac{3x^3}{3} + \frac{2x^2}{2} - x \right]_1^2$ <p>And simplified into</p> $[x^3 + x^2 - x]_1^2$	<p>Final Answer Allow for slips</p> <p>If they messed up in calculating their values in the substitution of the limits, still award marks.</p>		
4.4	2	<p>The function is a cyclic function, so we can find the area of one portion and multiply by 2.</p> $\int_{-2}^0 x^3 - 4x \, dx = \left[\frac{x^4}{4} - \frac{4x^2}{2} \right]_{-2}^0$ $= \left[\frac{x^4}{4} - 2x^2 \right]_{-2}^0$ $= [0] - [-4] = 4 \text{ units.}$ <p>Area of shaded region = 4×2 = 8 units²</p>	<p>Was able to integrate the function correctly.</p> $\frac{x^4}{4} - 2x^2$ <p>Some students will forget to take the absolute value of the negative area - or integrate the function from 2 to -2 - this will give the area of 0 units</p>	<p>Final Answer. 8 units.</p>		
4.5a	2	$a = (6 + 2t) \, m/s^2$ <p>Quarter of a minute = $\frac{1}{4} \times 60 \text{ sec} = 15 \text{ sec.}$</p> $a(15) = 6 + 2(15)$ $= 6 + 30$ <div style="border: 1px solid black; padding: 2px; display: inline-block;"> $= 36 \, m/s^2$ </div>	<p>Able to show that Quarter of a minute is t=15seconds</p> <p>If they substituted t=$\frac{1}{4}$ or t=0.25 into the acceleration formula.</p>	<p>Final answer.</p>		

			Or acceleration = 6.5m/s^2			
4.5b	3	$a = (6 + 2t) \text{ m/s}^2$ <p>First Integration:</p> $\int a = v(t) = \int (6 + 2t) dt$ $= 6t + 2 \frac{t^2}{2} + C$ $v(t) = 6t + t^2 + C$ <p>Using initial conditions to find C $v=0$ $t=2$</p> $0 = 6(2) + (2)^2 + C$ $\therefore C = 432$ $v(t) = 6t + t^2 + 432$ <p>Find velocity at $t=2$ sec</p> $v(2) = 6(2) + (2)^2 + 432$ $= 12 + 4 + 432$ $= 448 \text{ m/s}$	<p>Was able to integrate acceleration to get the velocity</p> $v(t) = 6t + t^2 + C$ <p>Any sign or evidence of integration shown: reward the student – even if it's wrong.</p>	<p>The initial conditions were used to find the constant: $C=432$,</p> <p>Hence the complete Velocity expression:</p> $v(t) = 6t + t^2 + 432$	Final Answer.	

Strand: 4 INTEGRATION

Item #	Skill level	Evidence (or expected answer)	Level 1	Level 2	Level 3	Level 4
4.6	4	$\frac{dN}{dt} \propto n$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $\frac{dN}{dt} = k n$ </div> $\frac{dN}{n} = k \cdot dt$ $\int \frac{dN}{n} = k \cdot \int dt$ $\ln N = kt + C$ $e^{\ln N} = e^{kt+C}$ $N = e^C \cdot e^{kt}$ $N = A_0 e^{kt}$ <p>Because radioactive DECAYS, k is NEGATIVE</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $N = A_0 e^{-kt}$ </div> <p>Because initial weight is 150 $\therefore A_0 = 150$</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $N = 150 e^{-kt}$ </div> <p>Half-life is the time where original breaks into half. $T_{1/2} = 435$ yrs into 75g</p> $75 = 150 e^{-k(435)}$ $\frac{1}{2} = e^{-435k}$ $\ln\left(\frac{1}{2}\right) = -435k$ $\therefore k = \frac{\ln 0.5}{-435} = 0.001593$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $N = 150 e^{-0.001593t}$ </div> <p>After 200 years $t = 200$</p> $N = 150 e^{-0.001593(200)}$ $N = 150 e^{-0.3186883589}$ $N = 150(0.72710211)$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 5px auto;"> $N = 109.065 \text{ g}$ </div>	<p>Shown evidence of separating differential equations</p> <p>Removing the proportional sign meant adding an "equal sign and k"</p> <p>Getting a general format for the Exponential Eqn:</p> $N = A_0 e^{kt}$ <p>Some will not derive, but write the general format straight away.</p>	<p>Was able to link the word DECAY which means "k" is NEGATIVE</p> $N = A_0 e^{-kt}$ <p>Or</p> $N = 150 e^{-kt}$	<p>Used initial conditions of half-life to get value of k</p> $k = \frac{\ln 0.5}{-435}$ $= 0.001593$	<p>Final Answer</p> <p>Be on the lookout if k has been rounded up to a particular decimal place. This will give several answers.</p>

Possible Solutions (depending on value of " k ")

- If $k = 0.002$ then $N = 100.548\text{g}$
- If $k = 0.0016$ then $N = 108.922\text{g}$
- If $k = 0.00159$ then $N = 109.140\text{g}$

THE END